

Objective: To construct the parent graphs of trigonometric functions for sine, cosine, and tangent using exact values.

Complete the following table for $\sin \theta$. Find the values of $\sin \theta$ for each angle.

θ (degree) x	0° 0π	30°	45°	60°	90° $\pi/2$	120°	135°	150°	180° π
$\sin \theta$ (nearest tenth), y	0/1 0	1/2 .5	$\sqrt{2}/2$.71	$\sqrt{3}/2$.87	1/1 1	$\sqrt{3}/2$.87	$\sqrt{2}/2$.71	1/2 .5	0/1 0

θ (degree) x	210°	225°	240°	270° $3\pi/2$	300°	315°	330°	360° 2π	390°
$\sin \theta$ (nearest tenth), y	-1/2 -.5	$-\sqrt{2}/2$ -.71	$-\sqrt{3}/2$ -.87	-1/1 -1	$-\sqrt{3}/2$ -.87	$-\sqrt{2}/2$ -.71	-1/2 -.5	0/1 0	1/2 .5

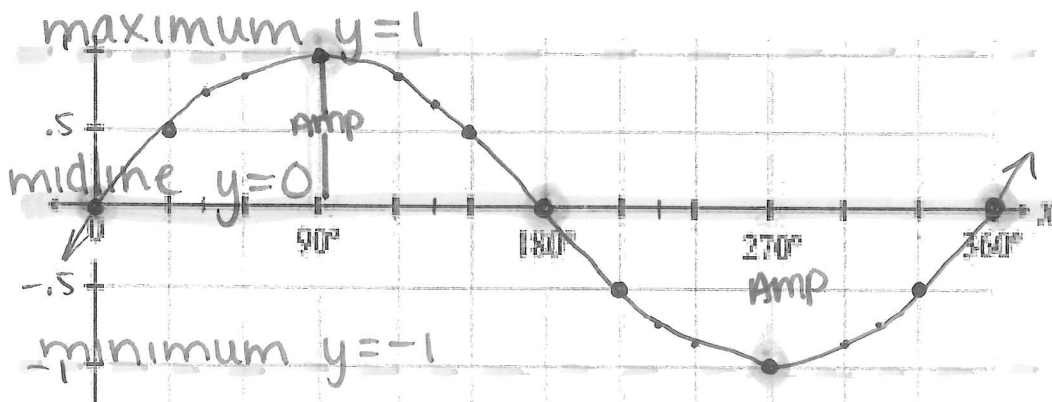
To graph the function $y = \sin \theta$, use values of θ expressed in either degrees or radians. These values represent the x values on a graph. Use the values of $\sin \theta$ expressed as a value rounded to the nearest tenth to represent the y values on the graph.

Ordered pairs for points on these graphs are of the form $(\theta, \sin \theta)$.

- $(0, 0)$
- $(30, .5)$
- $(45, .71)$
- $(60, .87)$
- $(90, 1)$
- \vdots

On the graph below, plot the points, $(\theta, \sin \theta)$. Connect the points with a smooth curve. This graph represents the graph of the sine function.

$y = \sin \theta \Rightarrow$ starts at midline



5 Key Pts

1. midline
2. max
3. midline
4. min
5. midline

- Period: one complete cycle of graph $\Rightarrow 360^\circ$ or 2π
- Amplitude: height/distance from midline to max/min $\Rightarrow \text{Amp} = 1$

Complete the following table for $\cos \theta$. Find the values of $\cos \theta$ for each angle.

θ (degree) x	0° 0π	30°	45°	60°	90° $\pi/2$	120°	135°	150°	180° π
$\cos \theta$ (nearest tenth), y	1/1 1	$\sqrt{3}/2$.87	$\sqrt{2}/2$.71	1/2 .5	0/1 0	-1/2 -.5	$-\sqrt{2}/2$ -.71	$-\sqrt{3}/2$ -.87	-1/1 -1

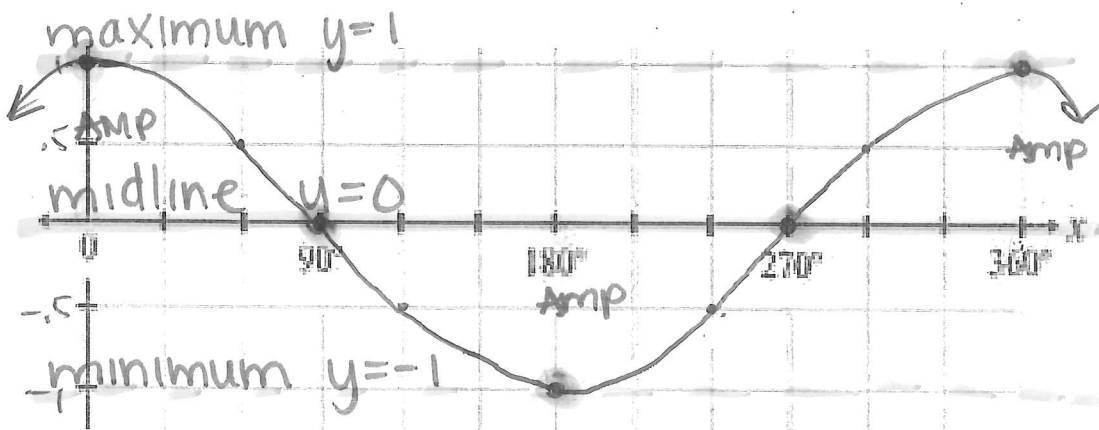
θ (degree) x	210°	225°	240°	270° $3\pi/2$	300°	315°	330°	360° 2π	390°
$\cos \theta$ (nearest tenth), y	$-\sqrt{3}/2$ -.87	$-\sqrt{2}/2$ -.71	-1/2 -.5	0/1 0	1/2 .5	$\sqrt{2}/2$.71	$\sqrt{3}/2$.87	1/1 1	$\sqrt{3}/2$.87

To graph the function $y = \cos \theta$, use values of θ expressed in either degrees or radians. These values represent the x values on a graph. Use the values of $\cos \theta$ expressed as a value rounded to the nearest tenth to represent the y values on the graph.

Ordered pairs for points on these graphs are of the form $(\theta, \cos \theta)$.

On the graph below, plot the points, $(\theta, \cos \theta)$. Connect the points with a smooth curve. This graph represents the graph of the cosine function.

$y = \cos \theta \Rightarrow$ starts at maximum



5 Key pts

1. max
2. midline
3. min
4. midline
5. max

• Period: one complete cycle 360° or 2π

• Amplitude: 1

$$\rightarrow \tan \theta = \frac{\sin \theta}{\cos \theta}$$

Complete the following table for $\tan \theta$. Find the values of $\tan \theta$ for each angle.

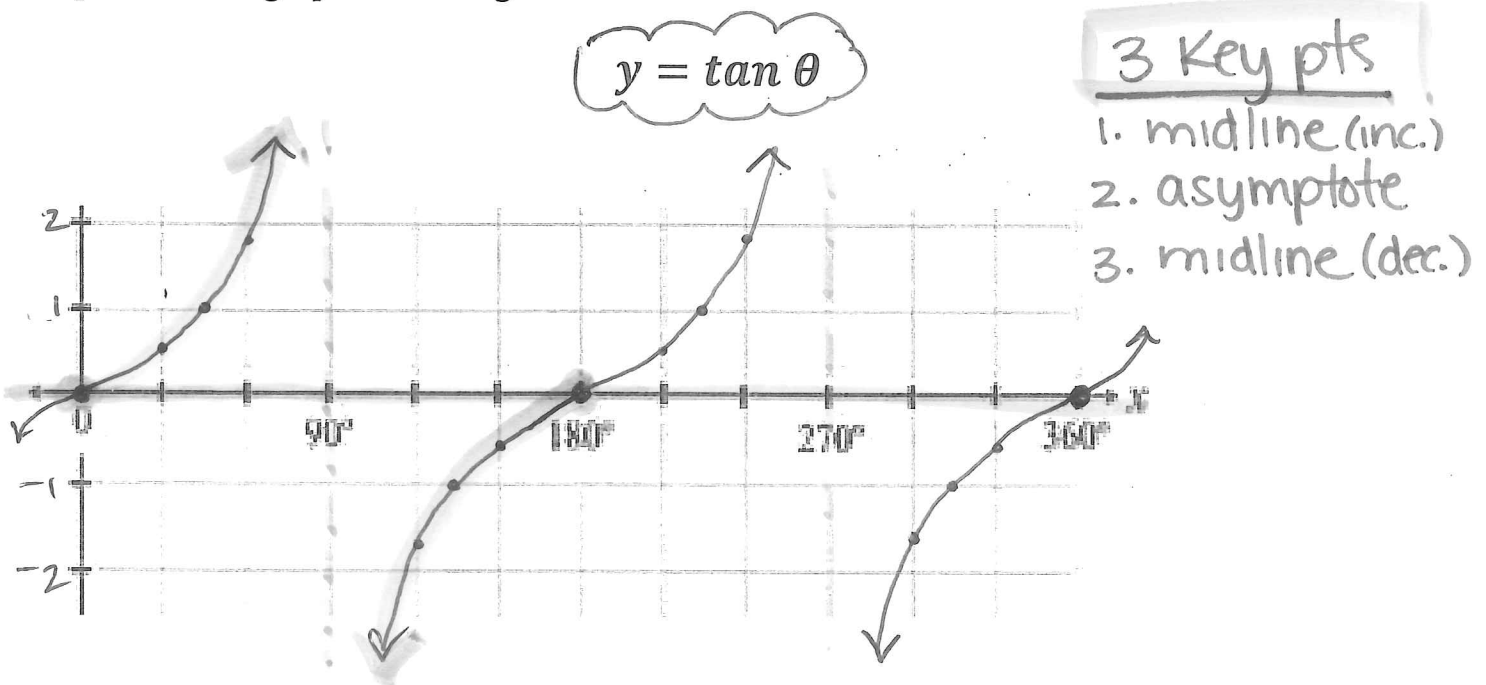
θ (degree) x	0°	30°	45°	60°	90°	120°	135°	150°	180°
$\tan \theta$ (nearest tenth), y	0/1 0	$1/2 \div \sqrt{3}/2$ $\frac{\sqrt{3}}{3} = .58$	$\sqrt{2}/2 \div \sqrt{2}/2$ 1	$\sqrt{3}/2 \div 1/2$ $\sqrt{3} = 1.73$	1/0 und.	$\sqrt{3}/2 \div -1/2$ $-\sqrt{3} = -1.73$	$\sqrt{2}/2 \div -\sqrt{2}/2$ -1	$1/2 \div -\sqrt{3}/2$ $-\frac{\sqrt{3}}{3} = -.58$	0/-1 0

θ (degree) x	210°	225°	240°	270°	300°	315°	330°	360°	390°
$\tan \theta$ (nearest tenth), y	$-1/2 \div -\sqrt{3}/2$ $\frac{\sqrt{3}}{3} = .58$	$-\sqrt{2}/2 \div -\sqrt{2}/2$ 1	$-\sqrt{3}/2 \div -1/2$ $\sqrt{3} = 1.73$	-1/0 und.	$-\sqrt{3}/2 \div 1/2$ $-\sqrt{3} = -1.73$	$-\sqrt{2}/2 \div \sqrt{2}/2$ -1	$-1/2 \div \sqrt{3}/2$ $-\frac{\sqrt{3}}{3} = -.58$	0/1 0	$1/2 \div \sqrt{3}/2$ $\frac{\sqrt{3}}{3} = .58$

To graph the function $y = \tan \theta$, use values of θ expressed in either degrees or radians. These values represent the x values on a graph. Use the values of $\tan \theta$ expressed as a value rounded to the nearest tenth to represent the y values on the graph.

Ordered pairs for points on these graphs are of the form $(\theta, \tan \theta)$.

On the graph below plot the points, $(\theta, \tan \theta)$. Connect the points with a smooth curve, but there should be breaks in the graph where there is an "error" or undefined value. This graph represents the graph of the tangent function.



- Period: 180° or $\pi \Rightarrow$ one complete cycle
- No Amplitude: no max or min
- Asymptotes occur at undefined values